

Problem 130B

Consider small amplitude, travelling water waves of wavelength, λ (wavenumber, $k = 2\pi/\lambda$), on an infinitely deep ocean of infinite horizontal extent. If the surface tension of the free surface is to be included in the analysis, find the propagation speed of the waves, c , in terms of the wavenumber, k , the surface tension, S , the fluid density, ρ , and the acceleration due to gravity, g . Assume planar, incompressible, inviscid and irrotational flow.