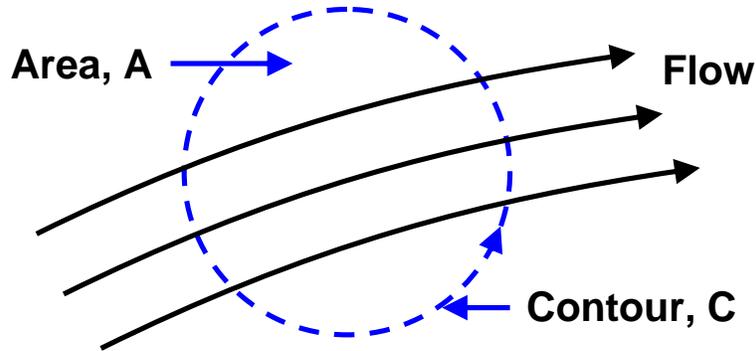


Problem 140A

Consider any closed contour, C , enclosing an area, A , in any planar incompressible flow (the area, A , contains only fluid):



The coordinate s is measured along the contour C and the “circulation”, Γ , is defined as the line integral of the fluid velocity, \underline{u} , around the contour C :

$$\Gamma = \int_C \underline{u} \cdot d\underline{s}$$

How is the circulation related to the vorticity of the flow inside the contour, C ?

Hint: Use Stokes' theorem:

$$\int_C \underline{u} \cdot d\underline{s} = \int_A \nabla \times \underline{u} \, dA$$