

Solution to Problem 301A:

1. The temperature at the stagnation point of the flow around the airplane, T_S , is related to the temperature far from the plane, T_∞ , by

$$\frac{T_S}{T_\infty} = 1 + \frac{U_\infty^2}{2c_p T_\infty} \quad (1)$$

where $U_\infty = 400m/s$ is the velocity of the airplane and c_p is the specific heat at constant pressure which is given by $c_p = \gamma\mathcal{R}/(\gamma - 1)$ where \mathcal{R} is the gas constant for air ($280m^2/s^2 \text{ }^\circ K$) and γ is the ratio of specific heats (1.4). This yields $T_S = 295^\circ K$.

2. The ratio of the pressure at the stagnation point, p_S , to that far from the airplane, p_∞ , assuming isentropic flow is given by

$$\frac{p_S}{p_\infty} = \left(\frac{T_S}{T_\infty} \right)^{\frac{\gamma}{\gamma-1}} = 3.11 \quad (2)$$

3. If the speed of the airplane is $1000m/s$, the stagnation temperature will be given by the first equation with $U_\infty = 1000m/s$ so

$$T_S = 723^\circ K \quad (3)$$