

Solution to Problem 303A:

An air blower takes air ($\mathcal{R} = 280\text{m}^2/\text{s}^2 \text{ }^\circ\text{K}$, $\gamma = 1.4$) from the atmosphere (pressure, $p_A = 100,000\text{kg}/\text{m}\cdot\text{s}^2$, temperature, $T_A = 293^\circ\text{K}$) and ingests it through a smooth entry duct so that the losses are negligible. The cross-sectional area of the entry duct just upstream of the blower and that of the exit duct are both 0.01m^2 . The pressure ratio, p_2/p_1 , across the blower itself is 1.05 and the exit pressure is equal to the atmospheric pressure, p_A . The air is assumed to behave isentropically upstream of the blower.

1. Since $p_2 = p_A$ and $p_2/p_1 = 1.05$ then $p_1/p_A = 1/1.05$ and since the upstream flow is isentropic:

$$\frac{T_1}{T_A} = \left(\frac{1}{1.05}\right)^{(\gamma-1)/\gamma} = \left(\frac{1}{1.05}\right)^{2/7} \quad (1)$$

and

$$c_p T_1 + u_1^2/2 = c_p T_A \quad (2)$$

therefore, the velocity of the air entering the blower is

$$u_1 = [2c_p T_A (1 - (1.05)^{-2/7})]^{1/2} = 89 \text{ m/s} \quad (3)$$

2. Since the density upstream $\rho_1 = \rho_A (p_1/p_A)^{1/\gamma} = 1.18\text{kg}/\text{m}^3$ the mass flow rate of air through the system is

$$\rho_1 u_1 A_1 = 1.18 \times 89 \times 0.01 = 1.05 \text{ kg/s} \quad (4)$$